Problem 14 $\S6.4$

Prove that for small x,

$$\frac{1}{x}\log(1+x) = 1 - \frac{x}{2} + \frac{x^2}{3} + \dots,$$
$$(1+x)^{\frac{1}{x}} = e(1 - \frac{x}{2} + \frac{11}{24}x^2 + \dots).$$
$$\frac{e - (1 + \frac{1}{n})^n}{1/n} \to \frac{e}{2} \text{ as } n \to \infty.$$

and hence that

Hence prove that